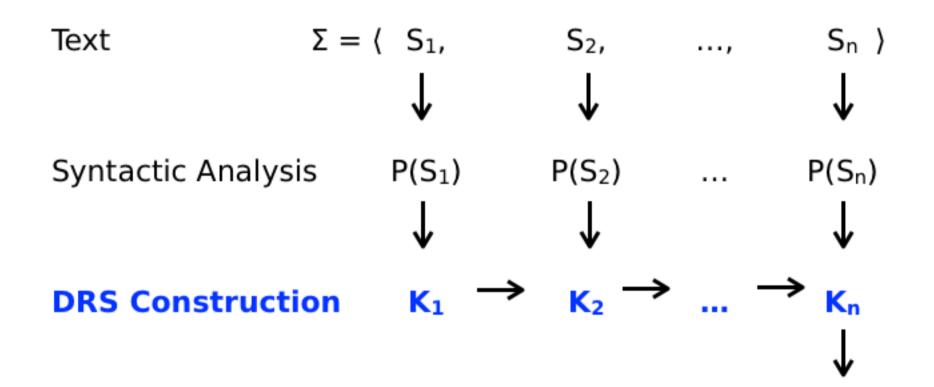
# Semantic Theory Lecture 14: Discourse Semantics II

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### **Discourse Representation Theory**



Interpretation by model embedding: Truthconditions of Σ

A farmer owns a donkey. He beats it.

x y z u
farmer(x)
donkey(y)
owns(x, y)
z = x
u = y
beat(z, u)

### **Denotational Interpretation**

Let

- $K = \langle U_K, C_K \rangle$  a DRS
- M = (U<sub>M</sub>, V<sub>M</sub>) a FOL model structure appropriate for K (i.e., M provides interpretations for all relation symbols occurring in K).
- An embedding of K into M is a function f from  $U_K$  to  $U_M$ .

# Verifying embedding

- An embedding f of K in M verifies K in M iff f verifies every condition  $\alpha \in C_{K}$ 
  - Notation:  $f \models_M K$
- **f verifies condition**  $\alpha$  in M (f  $\models_M \alpha$ ):
  - $f \models_M R(x_1, ..., x_n)$  iff  $(f(x_1), ..., f(x_n)) \in V_M(R)$
  - $f \models_M x = a$  iff  $f(x) = V_M(a)$
  - $f \models_M x = y$  iff f(x) = f(y)

# Truth

- Let K be a closed DRS and M be an appropriate model structure for K.
- **K** is true in M iff there is a verifying embedding f of K in M.

# Verifying Embedding: Example

Let K be the example DRS from above:

K = < {x, y, z, u},</p>

{professor(x), book(y), own(x,y), read(z,u), z=x, u=y} >

•  $f \models_M K$  iff f verifies every condition  $\alpha \in C_K$ , i.e.:  $f \models_M professor(x), f \models_M book(y) f \models_M, own(x,y),$  $f \models_M read(z,u), f \models_M z=x, and f \models_M u=y$ 

This holds iff:

 $f(x) \in V_M(\text{professor})$ ,  $f(y) \in V_M(\text{book})$ ,  $\langle f(x), f(y) \rangle \in V_M(\text{own})$ ,  $\langle f(z), f(u) \rangle \in V_M(\text{read})$ , f(z) = f(x), and f(u) = f(y)

# Simplification

■  $f(x) \in V_M(\text{professor}) \land f(y) \in V_M(\text{book}) \land \langle f(x), f(y) \rangle \in V_M(\text{own}) \land \langle f(z), f(u) \rangle \in V_M(\text{read}) \land f(z) = f(x) \land f(u) = f(y)$ 

iff

- $f(x) \in V_M(\text{professor}) \land f(y) \in V_M(\text{book}) \land \langle f(x), f(y) \rangle \in V_M(\text{own}) \land \langle f(x), f(u) \rangle \in V_M(\text{read}) \land f(u) = f(y)$
- $f(x) \in V_M(\text{professor}) \land f(y) \in V_M(\text{book}) \land \langle f(x), f(y) \rangle \in V_M(\text{own}) \land \langle f(x), f(u) \rangle \in V_M(\text{read}) \land f(u) = f(y)$

iff

■  $f(x) \in V_M(\text{professor}) \land f(y) \in V_M(\text{book}) \land \langle f(x), f(y) \rangle \in V_M(\text{own}) \land \langle f(x), f(y) \rangle \in V_M(\text{read})$ 

### Truth: Example

K = < {x, y, z, u},</p>

{professor(x), book(y), own(x,y), read(z,u), z=x, u=y} >

- Embedding f verifies K in M: f |=<sub>M</sub> K iff f verifies every condition  $\alpha \in C_K$ iff f(x)∈V<sub>M</sub>(professor) ∧ f(y)∈V<sub>M</sub>(book) ∧ ⟨f(x), f(y)⟩ ∈V<sub>M</sub>(own) ∧ ⟨f(x), f(y)⟩ ∈V<sub>M</sub>(read)
- **•** K is true in M iff there is an f such that  $f \models_M K$

# The Basic Contribution of DRT

- DRT provides an integrated model of global anaphoric relations (through DRS construction) and truth-conditional semantics (through model embedding).
- In particular, DRT models the ambivalent status of indefinite NPs: Indefinite noun phrases introduce new reference objects into context, and at the same time express existential quantification.

# Translation of DRSes to FOL

DRS K = 
$$\langle \{x_1, ..., x_n\}, \{c_1, ..., c_k\} \rangle$$

is truth-conditionally equivalent to the FOL formula: Ξ

$$\exists x_1 \dots \exists x_n [c_1 \land \dots \land c_k]$$

# Indefinite NPs and Conditionals

(1) If a student works, the professor is happy.

- (2)  $\exists x[student(x) \land work(x)] \rightarrow happy(the-professor)$
- (3)  $\forall x[student(x) \land work(x) \rightarrow happy(the-professor)]$

- Formulas (2) and (3) are logically equivalent:
- $\exists xA \rightarrow B \Leftrightarrow \forall x[A \rightarrow B]$  (provided that variable x does not occur free in B)

# Statives and Non-Statives: Linguistic Evidence

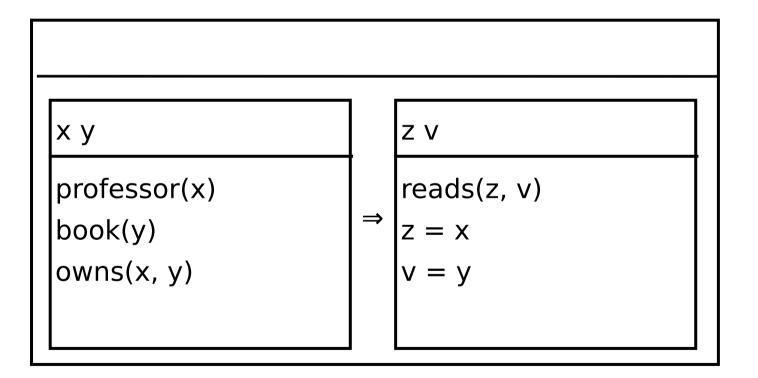
- If a student works, she will be successful.
- (1)  $\exists x[student(x) \land work(x)] \rightarrow successful(x)$
- (2)  $\exists x[student(x) \land work(x) \rightarrow successful(x)]$
- (3)  $\forall x[student(x) \land work(x) \rightarrow successful(x)]$

- Formula (1) is not closed (x occurs free)
- Formula (2) has wrong truth conditions (much too weak)
- Formula (3) is correct, but how can it be derived compositionally?

# Indefinite NPs in Hypothetical Text

- A car is parked in front of Bill's garage. Bill needs to get to the office quickly. He doesn't know who owns the car. He calls the police, and the car is towed away.
- Suppose a car is parked in front of Bill's garage. Bill needs to get to the office quickly. He doesn't know who owns the car. Then he will call the police, and the car will be towed away.
- Let a and b be two positive integers. Let b further be even.
  Then the product of a and b is even too.

# **DRS for Conditionals**



# DRS (1<sup>st</sup> Extension)

#### A discourse representation structure (DRS) K is a pair

- $(U_{K}, C_{K})$ , where
- U<sub>κ</sub> is a set of discourse referents
- C<sub>κ</sub> is a set of conditions

#### (Irreducible) conditions:

- R(u<sub>1</sub>, ..., u<sub>n</sub>) R n-place relation,  $u_i \in U_K$
- $\quad u = v \qquad \qquad u, v \in U_K$
- u = a  $u \in U_K$ , a is a proper name
- $K_1 \Rightarrow K_2$   $K_1$  and  $K_2$  DRSs
- Reducible conditions: as before

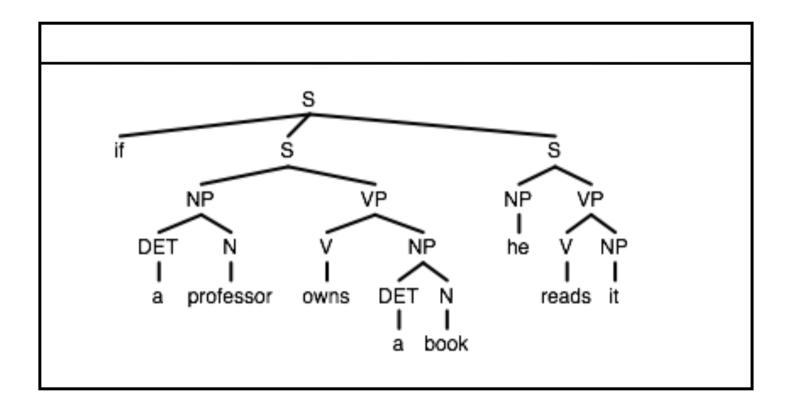
# Construction Rule for Conditionals

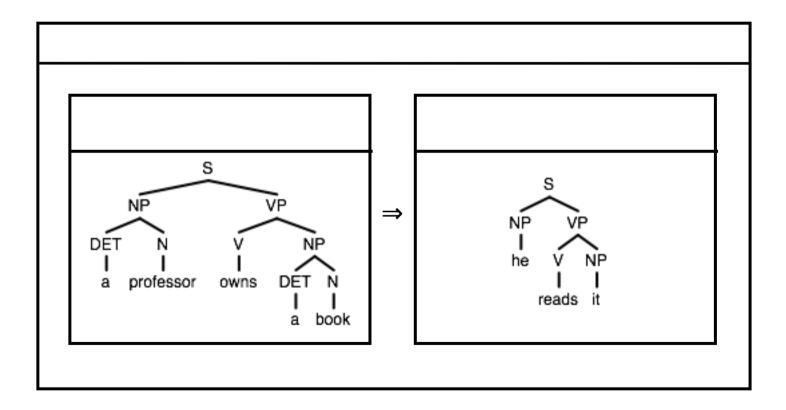
#### Triggering configuration:

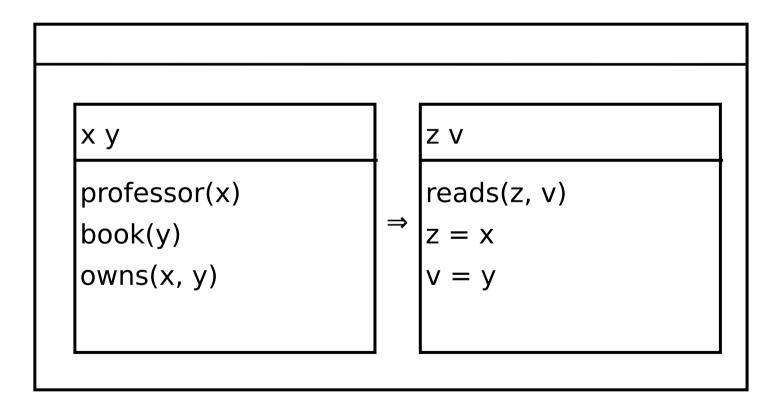
α is a reducible condition in DRS K of the form
 [s if [s β] (then) [s γ]]

#### Action:

- Remove  $\alpha$  from C<sub>K</sub>.
- Add  $K_1 \Rightarrow K_2$  to  $C_K$ , where
  - $K_1 = \langle \emptyset, \{ \beta \} \rangle$
  - $K_2 = \langle \emptyset, \{ \gamma \} \rangle$
- Remark:  $K_1 \Rightarrow K_2$  is called a **duplex condition**;  $K_1$  the "antecedent DRS" and  $K_2$  the "consequent DRS."







### **Embedding: Basic Version**

Let  $K = \langle U_K, C_K \rangle$  a DRS,  $M = \langle U_M, V_M \rangle$  an FOL model structure appropriate for K. An embedding of K into M is a function f from  $U_K$  to  $U_M$ .

An embedding f of K into M verifies K in M:  $f \models_M K$ 

iff f verifies every condition  $\alpha \in C_{K}$ .

f verifies condition  $\alpha$  in M (f  $\models_M \alpha$ ):

(i)  $f \models_M R(x_1, ..., x_n)$  iff  $\langle f(x_1), ..., f(x_n) \rangle \in V_M(R)$ (ii)  $f \models_M x = a$  iff  $f(x) = V_M(a)$ (iii)  $f \models_M x = y$  iff f(x) = f(y)

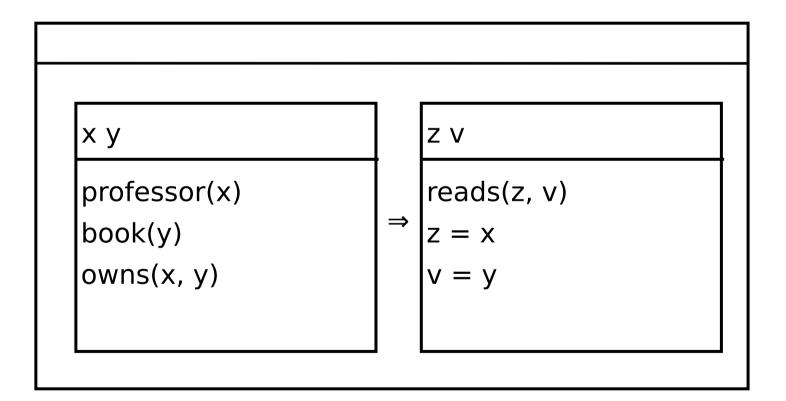
# Verifying Embedding for Duplex Conditions (Preliminary)

#### $f \models_M K_1 \Rightarrow K_2$

iff for all  $g \supseteq_{UK1} f$  such that  $g \models_M K_1$ , also  $g \models_M K_2$ 

■ We write  $g \supseteq_U f$  for " $g \supseteq f$  and Dom(g) = Dom(f)  $\cup$  U"

### This seems to work ...



# ... but in the general case, it doensn't

Mary knows a professor. If he owns a book, he gives it to a student.

s u					
s = Mary professor(u) know(s, u)					
	ху		ZVW		
	x = u		gives(z,v,w)		
	book (y)	⇒	z = x		
	owns (x, y)		v = y		
			student(w)		

# Verifying embedding for Duplex Conditions

#### ■ **f** ⊨<sub>M</sub> **K1** ⇒ **K2** iff

#### for all $g \supseteq_{U_{K_1}} f$ such that $g \models_M K_1$ , there is a $h \supseteq_{U_{K_2}} g$ such that $h \models_M K_2$

# Embedding (Revised)

Let U<sub>D</sub> a set of discourse referents,

$$\mathsf{K} = \langle \mathsf{U}_\mathsf{K}, \, \mathsf{C}_\mathsf{K} \rangle \text{ a DRS with } \mathsf{U}_\mathsf{K} \subseteq \mathsf{U}_\mathsf{D},$$

 $M = \langle U_M, V_M \rangle$  a FOL model structure appropriate for K.

An *embedding* of K into M is a (partial) function f from  $U_D$  to  $U_M$  such that  $U_K \subseteq$  Dom(f).

# Verifying Embedding: 1<sup>st</sup> Extension

An embedding f of K into M verifies K in M:  $f \models_M K$ 

iff f verifies every condition  $\alpha \in C_{K}$ .

f verifies condition  $\alpha$  in M (f  $\models_M \alpha$ ):

(i)  $f \models_M R(x_1, ..., x_n)$  iff  $\langle f(x_1), ..., f(x_n) \rangle \in V_M(R)$ 

iff

iff

(ii)  $f|_{=_M} x = a$  iff

(iii) 
$$f \mid_{=_M} x = y$$

$$(iv) \mathbf{f} \models_{\mathbf{M}} \mathbf{K}_1 \Rightarrow \mathbf{K}_2$$

$$f(x) = V_M(a)$$

$$f(x) = f(y)$$

for all  $g \supseteq_{V_{K_1}} f$  such that  $g \models_M K_1$ , there is a  $h \supseteq_{V_{K_2}} g$  such that  $h \models_M K_2$ 

# Definition of Truth, Revised

- Let K be a closed DRS and M be an appropriate model structure for K.
- K is true in M iff there is a verifying embedding f of K in M such that Dom(f) = U<sub>K</sub>.

# Construction Rule for Universal NPs

#### Triggering configuration:

- α is a reducible condition in DRS K; α contains a subtree [s [NP β] [VP γ]] or [VP [V γ] [NP β]]
- β = every δ

#### Action:

- Remove α from CK.
- Add  $K_1 \Rightarrow K_2$  to  $C_K$ , where
  - $K_1 = \langle \{x\}, \{\delta(x)\} \rangle$  and
  - $K_2 = \langle \emptyset, \{\alpha'\} \rangle$
  - obtain  $\alpha$ ' from  $\alpha$  by replacing  $\beta$  by x

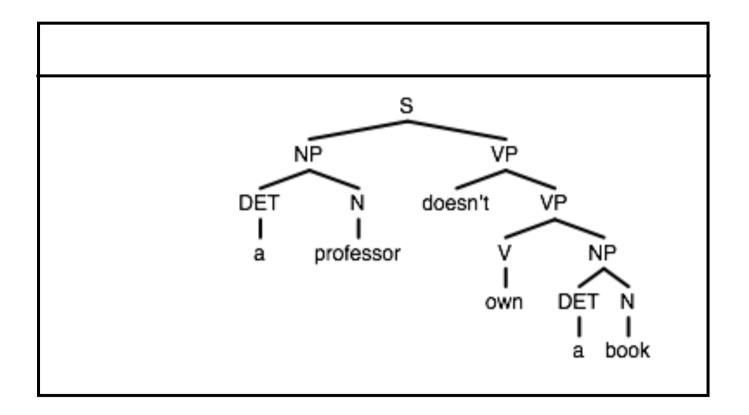
# **Construction Rule for Negation**

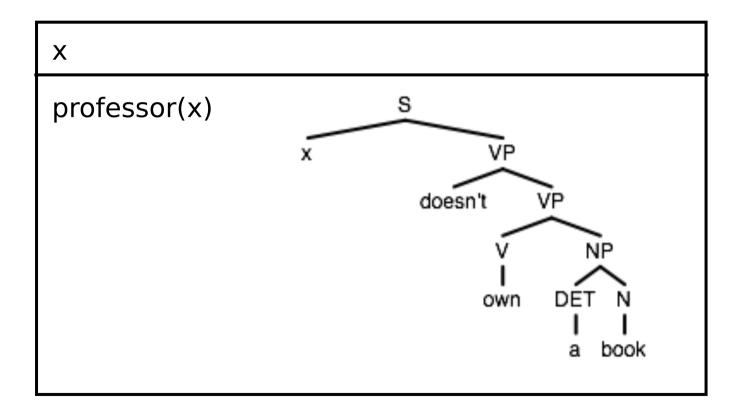
#### Triggering configuration:

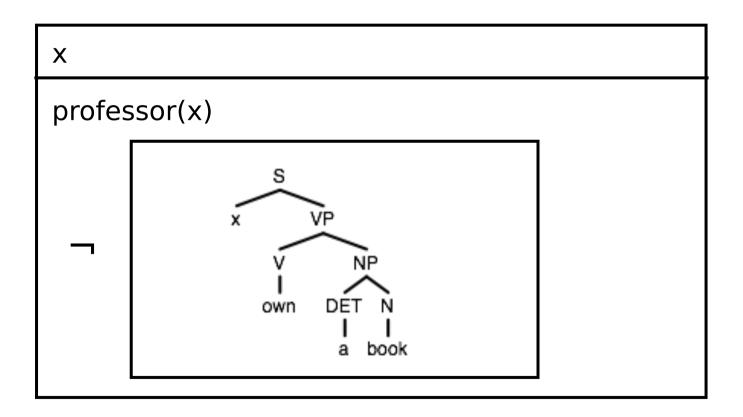
•  $\alpha$  is a reducible condition in DRS K of the form [s  $\beta$  [vp doesn't [vp  $\gamma$ ]]]

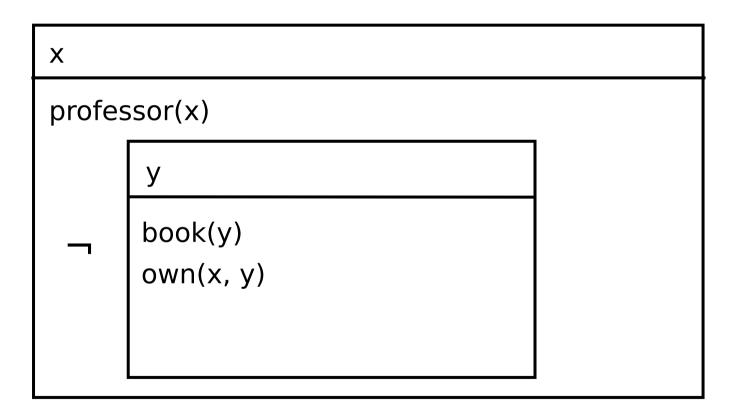
#### Action:

- Remove  $\alpha$  from C<sub>K</sub>
- Add  $\neg K_1$  to  $C_K$ , where  $K_1 = \langle \emptyset, \{ [s \ \beta [v_P \gamma]] \} \rangle$

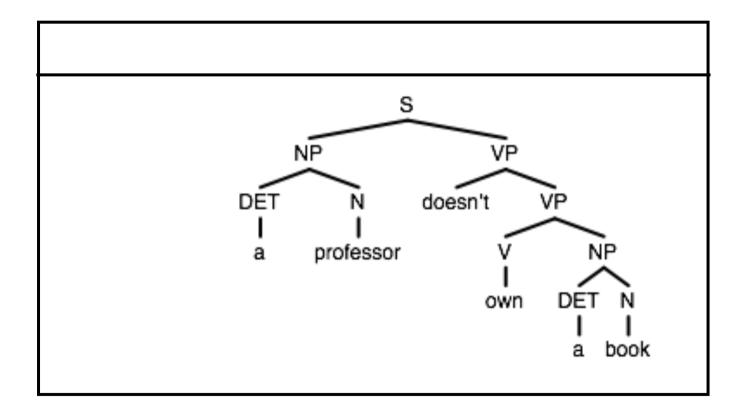




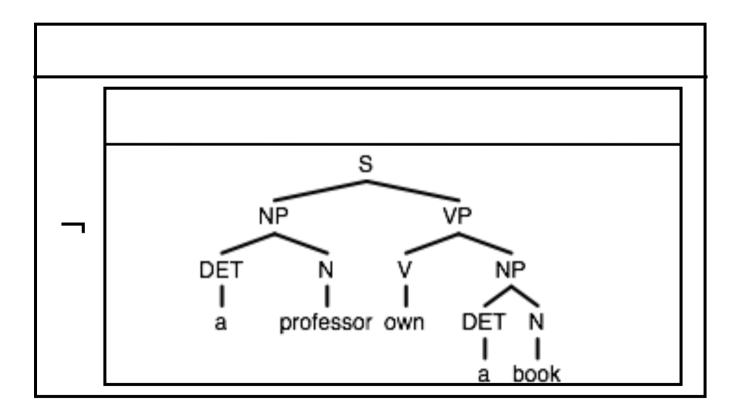




# Negation: Example, 2<sup>nd</sup> Reading



# Negation: Example, 2<sup>nd</sup> Reading



# Negation: Example, 2<sup>nd</sup> Reading

	ху	
-	professor(x) book(y) own(x, y)	

# Construction rule for clausal disjunction

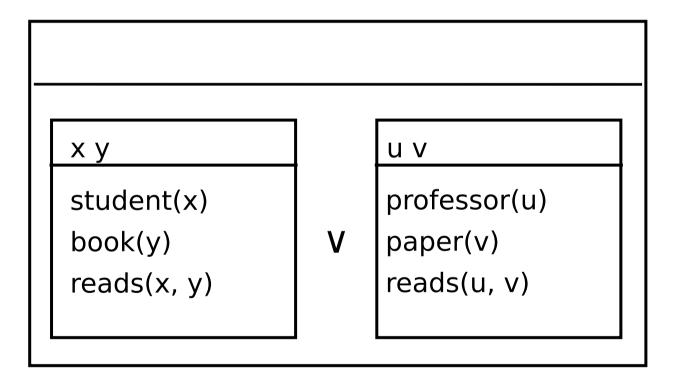
#### Triggering configuration:

•  $\alpha$  is a reducible condition in DRS K of the form [s [s  $\beta$ ] or [s  $\gamma$ ]]

#### Action:

- Remove α from C<sub>K</sub>
- Add K<sub>1</sub> v K<sub>2</sub> to C<sub>K</sub>, where
  - $K_1 = \langle \emptyset, \{\beta\} \rangle$  and
  - $K_2 = \langle \emptyset, \{\gamma\} \rangle$

A student reads a book, or a professor reads a paper.



# DRS: 2<sup>nd</sup> Extension

#### A discourse representation structure (DRS) K is a pair

- $(U_{K}, C_{K})$ , where
- U<sub>κ</sub> is a set of discourse referents
- C<sub>κ</sub> is a set of conditions

#### (Irreducible) conditions:

- **R**(u<sub>1</sub>, ..., u<sub>n</sub>) **R** n-place relation,  $u_i \in U_K$
- $u = v \qquad u, v \in U_K$
- u = a  $u \in U_K$ , a is a proper name
- $K_1 \Rightarrow K_2$   $K_1 \text{ and } K_2 \text{ DRSs}$
- $\blacksquare \neg K_1 \qquad \qquad K_1 \text{ DRS}$

# Verifying Embedding: 2<sup>nd</sup> Extension

An embedding f of K into M verifies K in M:  $f \models_M K$ 

iff f verifies every condition  $\alpha \in C_{K}$ .

f verifies condition  $\alpha$  in M (f  $\models_M \alpha$ ):

(i)  $f \models_M R(x_1, ..., x_n) \text{ iff } \langle f(x_1), ..., f(x_n) \rangle \in V_M(R)$ 

(ii) 
$$f|_{=_M} x = a$$
 iff  $f(x) = V_M(a)$ 

(iii) 
$$f \mid_{=_M} x = y$$
 iff  $f(x) = f(y)$ 

- (iv)  $f \models M K1 \Rightarrow K2$  iff for all  $g \supseteq_{U_{K1}} f$  such that  $g \models_M K_1$ , there is a  $h \supseteq_{U_{K2}} g$  such that  $h \models_M K_2$
- (v)  $\mathbf{f} \models_{\mathbf{M}} \mathbf{K_1 v K_2}$  iff there is a  $g_1 \supseteq_{UK1} \mathbf{f}$  such that  $g_1 \models_{\mathbf{M}} \mathbf{K_1}$ or there is a  $g_2 \supseteq_{UK2} \mathbf{f}$  such that  $g_2 \models_{\mathbf{M}} \mathbf{K_2}$

(vi)  $\mathbf{f} \models_{\mathbf{M}} \neg \mathbf{K}_{1}$  iff there is no  $g \supseteq_{UK1} \mathbf{f}$  such that  $g \models_{\mathbf{M}} \mathbf{K}_{1}$